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JEE MAIN-2020

COMPUTER BASED TEST (CBT)

DATE: 02-09-2020 (SHIFT-1) | TIME: (9.00 am to 12.00 pm)

Duration 3 Hours | Max. Marks: 300

QUESTION & SOLUTIONS

PART-A : PHYSICS

SECTION – 1 : (Maximum Marks : 80)

Single Choice Type

This section contains 20 Single choice questions. Each question has 4 choices (1), (2), (3) and (4) for its answer, out of which Only One is correct.

Full Marks : +4 If ONLY the correct option is chosen.

Negative Marks : -1 (minus one) mark will be deducted for indicating incorrect response.

1. A particle of mass m with an initial velocity $u\hat{i}$ collides perfectly elastically with a mass 3 m at rest. It moves with a velocity $v\hat{j}$ after collision, then v is given by

(1)
$$v = \sqrt{\frac{2}{3}}u$$
 (2) $v = \frac{u}{\sqrt{3}}$ (3) $v = \frac{1}{\sqrt{6}}u$ (4) $v = \frac{u}{\sqrt{2}}$

Ans. (4)

Sol. From momentum conservation

 $mu\hat{i} + 0 = mv\hat{j} + 3m\vec{v}'$

$$\vec{v}' = \frac{u}{3}\hat{i} - \frac{v}{3}\hat{j}$$

From kinetic energy conservation $\frac{1}{2}mu^2 = \frac{1}{2}mv^2 + \frac{1}{2}(3m)\left(\left(\frac{u}{3}\right)^2 + \left(\frac{v}{3}\right)^2\right)$

Solving $v = \frac{u}{\sqrt{2}}$

2. Two identical strings X and Z made of some material have tension T_x and T_z in then. If their fundamental frequencies are 450 Hz and 300 Hz, respectively, then the ratio T_x/T_z is :

(4) 2.25

(1) 1.25(2) 0.44 (3) 1.4

Sol. $f_x = -\frac{1}{2}$

$$f_y = \frac{1}{2\ell} \sqrt{\frac{T_y}{\mu}}$$

$$\frac{f_x}{f_y} = \frac{100}{300} = \sqrt{\frac{T_x}{T_y}}$$

 \Rightarrow T_x/T_y = 9/4 = 2.25

3. A cylindrical vessel containing a liquid is rotated about its axis so that the liquid rises at its sides as shown in the figure. The radius of vessel is 5 cm and the angular speed of rotation is ω rad s⁻¹. The difference in the height, h (in cm) of liquid at the centre of vessel and at the will be :

(1)
$$\frac{5\omega^2}{2g}$$
 (2) $\frac{2\omega^2}{25g}$
(3) $\frac{25\omega^2}{2g}$ (4) $\frac{2\omega^2}{5g}$



Ans. (3)

Sol. ρ



4. The least count of the main scale of a vernier callipers is 1 mm. Its vernier scale is divided into 10 divisions and coincide with 9 divisions of the main scale. When jaws are touching each other, the 7th division of vernier scale coincides with a division of main scale and the zero of vernier scale is lying right side of the zero of main scale. When this vernier is used to measure length of cylinder the zero of the vernier scale between 3.1 cm and 3.2 cm and 4th VSD coincides with a main scale division. The length of the cylinder is (VSD is vernier scale division)

(1) 2.99 cm (2) 3.07 cm (3) 3.21 cm (4) 3.2 cm

Ans. (2)

Sol. Zero Error = 0 + 7 × 0.1 = 0.070

Vernier reading = (3.1 + 4 × 0.01) – 0.07 = 3.07

5. A gas mixture consists of 3 moles of oxygen and 5 moles of argon at temperature T. Assuming the gases to be ideal and the oxygen bond to be rigid, the total internal energy (in units of RT) of the mixture is :

(1) 15 (2) 13 (3) 20 (4) 11

Ans. (1)

Sol. $\frac{f_1n_1RT_1}{2} + \frac{f_2n_2RT_2}{2} = 3 \times \frac{5}{2}RT + \frac{5}{2} \times 3RT = 15$

6. Interference fringes are observed on a screen by illuminating two thin slits 1 mm apart with a light source $(\lambda = 632.8 \text{ nm})$. The distance between the screen and the slits is 100 cm. If a bright fringe is observed on a screen at distance of 1.27 mm from the central bright fringe, then the path difference between the waves, which are reaching this point from the slits is close to :

(1) 2.87 (2) 2 nm (3) 1.27 μm (4) 2.05 μm

Ans. (3)

Sol. $\Delta P = dsin\theta$

=
$$d\theta$$

= $\frac{dy}{D} = \frac{10^{-3} \times 1.270 \text{ mm}}{1 \text{ m}} = 1.27 \mu \text{m}$

7. An amplitude modulated waves is represented by expression $v_m = 5 (1 + 0.6 \cos 6280t) \sin(211 \times 10^4 t)$ volts. The minimum and maximum amplitudes of the amplitude modulated wave are, respectively:

....(1)

....(2)

(1) 5V, 8V (2)
$$\frac{5}{2}$$
V,8V (3) 3V, 5V (4) $\frac{3}{2}$ V,5V

Ans. (2)

Sol. From given equation

$$\mu = 0.6$$

 $A_m = \mu Ac$

1

$$\frac{A_{max.} + A_{min.}}{2} = A_c = 5$$
$$\frac{A_{max.} - A_{min.}}{2} = 3$$
From Equation (1) + (2)

= 5

 $A_{max} = 8$ From Equation (1) - (2) $A_{min} = 2$

The mass density of a spherical galaxy varies as $\frac{K}{r}$ over a large distance 'r' from its center. In that 8. region, a small star is in a circular orbit of radius R. Then the period of revolution, T depends on R as :

(1)
$$T^2 \alpha \frac{1}{R^3}$$
 (2) $T^2 \alpha R$ (3) $T \alpha R$ (4) $T^2 \alpha R^3$

Ans. (2)

Sol.
$$M = \int \rho d^{1}$$

$$M = \int_{0}^{r=R_{0}} \frac{k}{r} 4\pi r^{2} dr$$

$$M = 4\pi k \int_{0}^{R_{0}} r dr$$

$$M = \frac{4\pi k R_{0}^{2}}{2} 2\pi k R^{2}$$

$$F_{G} = \frac{GMm}{R_{0}^{2}} = m\omega_{0}^{2}R$$

$$\Rightarrow \frac{G\frac{4\pi k R^{2}}{2}}{R^{2}} = \omega_{0}^{2}R \Rightarrow \omega_{0} = \sqrt{\frac{2\pi KG}{R}}$$

O

а

$$\therefore T = \frac{2\pi}{\omega_0} = \frac{2\pi\sqrt{R}}{\sqrt{2\pi KG}} = \sqrt{\frac{2\pi R}{KG}}$$
$$\Rightarrow T^2 \propto R$$

9. A beam of protons with speed 4×10^5 ms⁻¹ enters a uniform magnetic field of 0.3T at an angle of 60° to the magnetic field. the pitch of the resulting helical path of protons is close to : (Mass of the proton = 1.67×10^{-27} kg, charge of the proton = 1.69×10^{-19} C)

(1) 12 cm (2) 2 cm (3) 4 cm (4) 5 cm

Sol. Pitch = $(V\cos\theta)T$

$$= (V \cos \theta) \frac{2\pi m}{eB}$$

= $(4 \times 10^5 \cos 60^\circ) \frac{2\pi}{0.3 \times 10} \left(\frac{1.67 \times 10^{-27}}{1.69 \times 10^{19}} \right)$
= 4 cm

A uniform cylinder of mass M and radius R is to be pulled over a step of height a (a < R) by applying a force F at its centre 'O' perpendicular to the plane through the axes of the cylinder on the edge of the step (see figure). The minimum value of F required is :

(1)
$$Mg \sqrt{1 - \left(\frac{R - a}{R}\right)^2}$$
 (2) $Mg \sqrt{1 - \frac{a^2}{R^2}}$
(3) $Mg \sqrt{\left(\frac{R}{R - a}\right) - 1}$ (4) $Mg \frac{a}{R}$

Ans. (1)

Ans. Sol.

Sol. FR > mg $\cos\theta R$

 $F > mgcos\theta$

$$F > mg \frac{\sqrt{R^2 - (R - a)^2}}{R} \Rightarrow Mg \sqrt{1 - \left(\frac{R - a}{R}\right)^2}$$

11. A bead of mass m stays at point P (a, b) on a wire bent in the shape of a parabola $y = Cx^2$ and rotating with angular speed ω (see figure). The value of ω is (neglect friction)

(1)
$$\sqrt{2gC}$$

(2) $\sqrt{\frac{2gC}{ab}}$
(3) $\sqrt{\frac{2g}{C}}$
(4) $2\sqrt{2gC}$
(4) $m\omega^2 a \cos\theta = mgsin\theta$



A charged particle (mass m and charge q) moves along X axis with velocity V₀. When it passes through the origin it enters a region having uniform electric field E
 = -Eĵ which extends upto x = d. Equation of path of electron in the region x > d is :

(1)
$$y = \frac{qEd}{mV_0^2}x$$
 (2) $y = \frac{qEd}{mV_0^2}(x-d)$
(3) $y = \frac{qEd}{mV_0^2}\left(\frac{d}{2} - x\right)$ (4) $y = \frac{qEd^2}{mV_0^2}x$

Ans. (3)

Sol. x > d path is straight line

$$\frac{-y = \frac{1}{2}at^2}{x - d} = \frac{at}{V_0}$$
$$\frac{-y - \frac{1}{2}at^2}{at} = \frac{x - \frac{1}{V_0}}{V_0}$$

 $\frac{-y}{at} - \frac{1}{2}\frac{d}{V_0} = \frac{x}{V_0} - \frac{d}{V_0}$



$$\frac{-myV_0}{qEd} = \frac{x}{V_0} - \frac{d}{2V_0}$$
$$y = \frac{-qEd}{mV_0} \left(\frac{x}{V_0} - \frac{d}{2V_0}\right)$$
$$y - = \frac{qEd}{mV_0^2} \left(\frac{d}{2} - x\right)$$

14. In a reactor, 2 kg of $_{92}U^{235}$ fuel is fully used up in 30 days. The energy released per fission is 200 Mev. given that the Avogadro number, N = 6.023×10^{26} per kilo mol and 1 eV = 1.6×10^{-19} J. The power output of the reactor is close to :

(1) 54 MW (2) 60 MW (3) 125 MW (4) 35 MW

Ans. (2)

Sol. $P = \frac{E}{t}$

 $=\frac{2}{235}\times\frac{60.23\times10^{26}\times200\times1.6\times10^{-19}}{30\times24\times60\times60}=60W$

15. A plane electromagnetic wave, has frequency of 2.0×10^{10} Hz and its energy density is 1.02×10^{-8} J/m³ in vacuum. The amplitude of the magnetic field of the wave is close to $\left(\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2}\right)$ and speed

of light = 3 × 10⁸ ms⁻¹) :

(1) 160 nT (2) 180 nT (3) 190 nT (4) 150 nT

Ans. (1)

Sol. Energy Density $= \frac{1}{2} \frac{B^2}{\mu_0}$

 $B = \sqrt{2 \times \mu_0 \times Energy density}$

 $B = \sqrt{2 \times 4\pi \times 10^{-7} \times 1.02 \times 10^{-8}} = 160 \times 10^{-9} = 160 \text{ nT}$

- 16. Train A and train B are running on parallel tracks in the opposite directions with speed of 36 km/hour and 72 km/hour, respectively. A person is walking in train A in the direction opposite to its motion with a speed of 1.8 km/hour. Speed (in ms⁻¹) of this person as observed from train B will be close to : (take the distance between the tracks as negligible)
 - (1) 30.5 ms⁻¹ (2) 29.5 ms⁻¹ (3) 31.5 ms⁻¹ (4) 28.5 ms⁻¹
- **Ans.** (2)
- **Sol.** $V_A = 36 \text{ km/hr} = 10 \text{ m/s}$

 $V_{B} = -72 \text{ km/hr} = -20 \text{ m/s}$ $V_{MA} = -1.8 \text{ km/hr} = -0.5 \text{ m/s}$ $V_{man, B} = V_{man, A} + V_{A, B}$ $= V_{man, A} + V_{A} - V_{B}$ = -0.5 + 10 - (-20)= -0.5 + 30

= 29.5 m/s

17. Magnetic materials used for making permanent magnets (P) and magnets in a transformer (T) have different properties of the following, which property best matches for the type of magnet required ?

(1) T : Large retentivity, large coercivity

- (2) P : Large retentivity, large coercivity
- (3) T : Large retentivity, small coercivity
- (4) T : Small retentivity, large coercivity

- **Ans.** (2)
- Sol. Based on theory
- **18.** Shown in the figure is rigid and uniform one meter long rod AB held in horizontal position by two strings tied to its ends and attached to the ceiling. The rod is of mass 'm' and has another weight of mass 2m hung at a distance of 75 cm from A. The tension in the string at A is :



 $\rho_{\rm C} = 1.724 \times 10^{-8}$

 $\rho_{\rm T} = 5.65 \times 10^{-8}$

20. A spherical mirror is obtained as shown in the figure from a hollow glass sphere. if an object is positioned infront of the mirror, what will be the nature and magnification of the image of the object? (Figure drawn as schematic and not to scale)



SECTION – 2 : (Maximum Marks : 20)

This section contains FIVE (05) questions. The answer to each question is NUMERICAL VALUE with two digit integer and decimal upto one digit.

If the numerical value has more than two decimal places truncate/round-off the value upto TWO decimal places.

FOUNDATIC

Full Marks : +4 If ONLY the correct option is chosen.

Zero Marks : 0 In all other cases

A 5µF capacitor is charged fully by a 220 V supply. It is then disconnected from the supply and is 21. connected in series to another uncharged 2.5 µF capacitor. If the energy change during the charge

redistribution is $\frac{X}{100}$ J then value of X to the nearest integer is :

Ans. (36)

 $C_1 = 5 \mu F$ Sol. V₁ = 220 volt C₁ – əμ⊢ C₂ = 2.5 μF $V_2 = 0$ Heat loss; $\Delta H - U_i - U_f = \frac{1}{2} \frac{c_1 c_2}{c_1 + c_2} (v_1 - v_2)^2$ $=\frac{1}{2} \times \frac{5 \times 2.5}{(5+2.5)} (220-0)^2 \mu J$ $=\frac{5}{2\times3}\times22\times22\times100\times10^{-6}$ J $=\frac{5\times11\times22}{3}\times10^{-4}\,J=\frac{55\times22}{3}\times10^{-4}\,J$ $=\frac{1210}{3}\times 10^{-4} \, J=\frac{1210}{3}\times 10^{-3} \, J=4\times 10^{-2}$ T-JEE

According to questions

$$\frac{x}{100} = 4 \times 10^{-2}$$

So, x = 4

Note: But given answer by JEE Main x = 36

22. A small block starts slipping down from a point B on an inclined plane AB, which is making an angle heta with the horizontal section BC is smooth and the remaining section CA is rough with a coefficient of friction µ. It is found that the block comes to rest as it reaches the bottom (point A) of the inclined plane. If BC = 2AC, the coefficient of friction is given by μ = ktan θ . The value of k is



Ans. (3)

Let AC = ℓ BC = 2ℓ $AB = 3\ell$ Sol. *.*.. ÷.

Apply work - Energy theorem W_{f} + W_{mg} = ΔKE В mg (3ℓ) sin θ – μ mgcos $\theta(\ell)$ = 0 + 0 μ mgcos $\theta \ell$ = 3mg ℓ sin θ $3\ell sin \theta$ Rough С $\mu = 3 \tan \theta = k \tan \theta$ k = 3 *.*..

23. An engine takes in 5 moles of air at 20°C and 1 atm, and compresses it adiabatically to 1/10th of the original volume. Assuming air to be a diatomic ideal gas made up of rigid molecules, the change in its internal energy during this process comes out to be XkJ. The value of X to the nearest integer is :

Sol.
$$T_1 V_1^{\gamma - 1} = T_2 V_2^{\gamma - 1}$$

 $T_2 = T_1 \left(\frac{V_1}{V_2}\right)^{\gamma - 1}$
 $= T_1 (10)^{\frac{7}{5} - 1}$
 $T_2 = T_1 (10)^{2/5}$
 $\Delta V = \frac{5}{2} nR; \frac{5}{2} \times 5 \times 3[10^{2/5} - 1](293)$
 $\frac{625}{6} \times 1.5 \times 293 = 461440$
 $\approx 46 \text{ ks}$

When radiation of wavelength A is used to illuminate a metallic surface, the stopping potential is V. 24. When the same surface is illuminated with radiation of wavelength 3A, the stopping potential is $\frac{V}{4}$. If the threshold wavelength for the metallic surface is $n\lambda$ then value of n will be :

hr

Sol.

$$\frac{hc}{\lambda} = \phi + eV \qquad \dots (1)$$

$$\frac{hc}{3\lambda} = \phi + \frac{eV}{4} \qquad \dots (2)$$
from (1) & (2)
$$\frac{hc}{\lambda} \left(1 - \frac{1}{3}\right) = \frac{3}{4}eV$$

$$\frac{hc}{\lambda} \frac{2}{3} = \frac{3}{4}eV$$

$$eV = \frac{8}{9}\frac{hc}{\lambda}$$

$$\frac{hc}{\lambda} = \phi + \frac{8}{9}\frac{hc}{\lambda}$$

(2)

$$\begin{split} \varphi &= \frac{hc}{9\pi} = \frac{hc}{\lambda_{th}} \\ \lambda_{th} &= 9\lambda \\ \therefore \qquad k = 9 \end{split}$$

25. A circular coil of radius 10 cm is placed in a uniform magnetic field of 3.0 × 10⁻⁵ T with its plane perpendicular to the field initially. It is rotated at constant angular speed about an axis along the diameter of coil and perpendicular to magnetic field so that it undergoes half of rotation in 0.2 s. The maximum value of EMF induced (in µV) in the coil will be close to the integer...

Flux as a function of time $\phi = \vec{B} \cdot \vec{A} = AB\cos(\omega t)$ Sol.

Emf induced,

$$e = \frac{-d\phi}{dt} = AB\omega \sin(\omega t)$$

Max. value of Emf = AB ω

$$= \pi R^2 B \omega$$

Max. value of Emf = AB
$$\omega$$

= $\pi R^2 B \omega$
= $3.14 \times 0.1 \times 0.1 \times 3 \times 10^{-5} \times \frac{\pi}{0.2} = 15$

PART-B : CHEMISTRY

SECTION - 1 : (Maximum Marks : 80)

Single Choice Type

This section contains 20 Single choice questions. Each question has 4 choices (1), (2), (3) and (4) for its answer, out of which Only One is correct.

Full Marks : +4 If ONLY the correct option is chosen.

Negative Marks : -1 (minus one) mark will be deducted for indicating incorrect response.

26. The figure that is not a direct manifestation of the quantum nature of atom is :



27. Which one of the following graphs is not correct for ideal gas?



d = Density, P = Pressure, T = Temperature

Ans. (4)

Sol. For ideal gas

PM = dRT

$$d = \left\lceil \frac{PM}{R} \right\rceil \frac{1}{T}$$

So graph between d Vs T is not straight line.

28. For the following Assertion and Reason, the correct option is

Assertion (A) : When Cu (II) and sulphide ions are mixed, they react together extremely quickly to give a solid.

Reason (R) : The equilibrium constant of Cu^{2+} (aq) + S^{2-} (aq) \Box CuS(s) is high because the solubility product is low.

(1) (A) is false and (R) is true.

(2) Both (A) and (R) are false.

(3) Both (A) and (R) are true but (R) is not the explanation for (A).

(4) Both (A) and (R) are true and (R) is the explanation for (A).

Ans. (3)

- **Sol.** Rate of chemical reaction has nothing to do with value of equilibrium constant.
- **29.** The major product in the following reaction is :





(3) Ionization enthalpy (4) Atomic radius

Ans.	(4)	
Sol.	On moving Left to Right along a period.	
	Atomic Radius \Rightarrow decreases.	
	Electronegativity \Rightarrow Increases.	
	Electron gainenthalpy \Rightarrow Increases.	
	Ionisation Enthalpy \Rightarrow Increases.	
36.	For octahedral Mn(II) and tetrahedral Ni(II) com	plexes, consider the following statements :
	(I) both the complexes can be high spin.	
	(II) Ni(II) complex can very rarely be of low spin	
	(III) with strong field ligands, Mn(II) complexes o	an be low spin.
	(IV) aqueous solution of Mn(II) ions is yellow in	color.
	The correct statements are :	
	(1) (I) and (II) only	(2) (I), (II) and (III) only
	(3) (I), (III) and (IV) only	(4) (II), (III) and (IV) only
Ans.	(2)	
Sol.	With weak field ligands Mn(II) will be of high spi	n and with strong field ligands it will be of low spin. Ni(II)
	tetrahedral complexes will be generally of high	spin due to sp ³ hybridisation. Mn(II) is of light pink color
	in aqueous solution.	
37.	In Carius method of estimation of halogen, 0.1	72 g of an organic compound showed presence of 0.08
	g of bromine. Which of these is the correct strue	cture of the compound ?
		NH ₂ NH ₂
		Br
	(1) H_3C -Br (2) H_3C -C H_2 -Br	(3) (4)
		Br Br
Ans.	(3)	
Sol.	Mol of Bromine = $\frac{0.08}{220}$ = 10 ⁻³ mol	
	80	
	Molar mass of compound = $\frac{0.172}{M} = 10^{-3}$	
	0 172	
	$M = \frac{3172}{10^{-3}} = 172g$	
	NH ₂	
	Molar mass of = 80 + 72 + 6 + 14 = 17	2 g
	Br	

38. An open beaker of water in equilibrium with water vapour is in a sealed container. When a few grams of glucose are added to the beaker of water, the rate at which water molecules :

(1) leaves the vapour decreases

- (2) leaves the solution decreases
- (3) leaves the vapour increases (4) leaves the solution increases

Ans. (3)

- Sol. The vapour pressure of solution will be less than vapour pressure of pure solvent, so some vapour molecules will get condensed to maintain new equilibrium.
- 39. The statement that is not true about ozone is :

(1) in the stratosphere, CFCs release chlorine free radicals (CI) which reacts with O₃ to give chlorine dioxide radicals.

- (2) in the stratosphere, it forms a protective shield against UV radiation.
- (3) it is a toxic gas and its reaction with NO gives NO₂
- (4) in the atmosphere, it is depleted by CFCs.
- Ans. (1)
- Sol. In presence of sunlight CFC's molecule divides & release chlorine free radical, which react with ozone give chlorine monoxide radical (CIO*) and oxygen. UNDAT

 $CF_2Cl_2(g) \xrightarrow{UV} \dot{C}l(g) + \dot{C}F_2Cl(g)$ $Cl^{\bullet}(g) + O_{3}(g) \longrightarrow ClO^{\bullet}(g) + O_{2}(g)$ $CIO^{\bullet}(q) + O(q) \longrightarrow CI^{\bullet}(q) + O_{2}(q)$

- 40. The metal mainly used in devising photoelectric cells is :
 - (1) Li (2) Rb (3) Cs (4) Na
- Ans. (3)
- Cesium has lowest ionisation enthalpy and hence it can show photoelectric effect to the maximum extent Sol. hence it is used in photo electric cell.
- 41. Which of the following is used for the preparation of colloids?
 - (1) Ostwald process (2) Van Arkel Method (3) Mond Process (4) Bredig's Arc Method
- Ans. (4)
- Bredig's Arc Method is used for preparation of colloidal sol's of less reactive metal like Au, Ag, Pt. Sol.

42. Consider that d⁶ metal ion (M²⁺) forms a complex with agua ligands, and the spin only magnetic moment of the complex is 4.90 BM. The geometry and the crystal field stabilization energy of the complex is : (1) tetrahedral and $-1.6\Delta_t + 1P$ (2) octahedral and $-2.4\Delta_0 + 2P$

- (3) tetrahedral and $-0.6\Delta_t$ (4) octahedral and $-1.6\Delta_0$
- Ans. (3)
- Sol. Since spin only magnetic moment is 4.90 BM so number of unpaired electrons must be 4. so If the complex is octahedral, then it has to be high spin complex with configuration $t_{2a^{21.1}}e_{a^{1.1}}$ in that case

CFSE = 4 X ($-0.4\Delta_0$) + 2 X $0.6\Delta_0$ = $-0.4\Delta_0$

If the complex is tetrahedral then its electronic configuration will be $= e_{a^{2,1}}t_{2a^{1,1,1}}$ and CFSE will be = 3 X

 $(-0.6\Delta_t)$ + 3 X $(0.4\Delta_t)$ = $-0.6\Delta_t$

- **43.** If AB₄ molecule is a polar molecule, a possible geometry of AB₄ is :
 - (1) Square pyramidal

(2) Rectangular planar

(3) Square planar

(4) Tetrahedral

- **Ans**. (1)
- **Sol.** For AB₄ compound possible geometry are

S. No.	Bond Pair	Lone pair	Total	Hybridisation	Geometry	Polarity
1	4	0	4	sp ³	Tetrahedral	non polar
2	4	1	5	sp³d	sea-saw	polar
3	4	2	6	dp ³ d ²	square planar	non polar

Square pyramidal can be polar due to lone pair moment as the bond pair moments will get cancelled out.

44. The IUPAC name for the following compound is :



- (1) 2, 5-dimethyl-6-carboxy-hex-3-enal
- (2) 2, 5-dimethyl-5-carboxy-hex-3-enal
- (3) 6-formyl-2-methyl-hex-3-enoic

Т² СООН -enoic (4) 2, 5-dimethyl-6-oxo-hex-3-enoic acid

Ans. (4)

Sol. 🗸

⁶CHO

(2, 5-dimethyl-6-oxo-hex-3-enoic acid

45. Consider the following reactions :

(i) Glucose + ROH \xrightarrow{dryHCl} Acetal $\xrightarrow{x \text{ eq. of}}$ acetyl derivative

(ii) Glucose $\xrightarrow{\text{Ni/H}_2} A \xrightarrow{\text{y eq. of}} acetyl derivative$

- (iii) Glucose $\xrightarrow{z \text{ eq. of}}_{(CH_3CO)_2O}$ acetyl derivative
- 'x', 'y' and 'z' in these reactions are respectively.

(1) 5, 6 & 6	(2) 4, 5 & 5	(3) 4, 6 & 5	(4) 5, 4 & 5
() =) = = =	() ,		() = ;

Ans. (3)



Slope=2

loak=0.477

logP

SECTION – 2 : (Maximum Marks : 20)

This section contains FIVE (05) questions. The answer to each question is **NUMERICAL VALUE** with two digit integer and decimal upto one digit.

If the numerical value has more than two decimal places truncate/round-off the value upto TWO decimal places.

Full Marks : +4 If ONLY the correct option is chosen.

Zero Marks : 0 In all other cases

46. The mass of gas adsorbed, x, per unit mass of adsorbate, m, was measured at various pressures, p. A

graph between $\log \frac{x}{m}$ and log p gives a straight line with slope equal to 2 and the intercept equal to

log

0.4771. The value of $\frac{x}{m}$ at a pressure of 4 atm is :

(Given log 3 = 0.4771)

Ans. (NTA Answer is given 6)

Sol. $\left(\frac{x}{m}\right) = k(P)^{\frac{1}{n}}$

$$\left(\frac{x}{m}\right) = k(P)^{\frac{1}{n}} \log\left(\frac{x}{m}\right) = \log k + \frac{1}{n} \log P$$

Slope
$$=\frac{1}{n}=2$$

Intercept \Rightarrow logk = 0.477 So k = Antilog (0.477) = 3

So
$$\left(\frac{\mathbf{x}}{\mathbf{m}}\right) = \mathbf{k}(\mathbf{P})^{\mathbf{x}}$$

= 3[4]² = 48

47. The oxidation states of iron atoms in compounds (A), (B) and (C), respectively, are x, y and z. The sum of x, y and z is

$$Na_{4}[Fe(CN)_{5}(NOS)]$$
 $Na_{4}[FeO_{4}]$ $Fe_{2}(CO)_{9})$

Ans. (6)

Sol. The oxidation states of iron in these compounds will be

A = +2 B = +4

C = 0

The sum of oxidation states will be = 6.

48. The internal energy change (in J) when 90 g of water undergoes complete evaporation at 100°C is.....

(Given : ΔH_{vap} for water at 373 K = 41 kJ/mol, R = 8.314 JK⁻¹ mol⁻¹)

Ans. (189494)

Sol. $\Delta H = \Delta U + \Delta ngRT$

41000 X 5 = ∆U + 5 X 8.314 X 373 $205000 = \Delta U + 15505.61$ ∆U = 189494.39 J = 189494 J

49. The Gibbs energy change (in J) for the given reaction at $[Cu^{2+}] = [Sn^{2+}] = 1$ M and 298 K is : $Cu(s) + Sn^{2+}(aq.) \rightarrow Cu^{2+}(aq.) + Sn(s);$

($E^{0}_{\text{Sn}^{2+}|\text{Sn}} = -0.16V, E^{0}_{\text{Cu}^{2+}|\text{Cu}} = 0.34V, \ \text{Take F} = 96500 \ \text{C} \ \text{mol}^{-1}\text{)}$

- Ans. (96500)
- $\mathsf{E}^{0}_{cell} = \mathsf{E}^{0}_{Sn^{2^{+}}/Sn} \mathsf{E}^{0}_{Cu^{2^{+}}/Cu}$ Sol. = -0.16 - 0.34= - 0.50 V
 - $\Delta G^0 = -nFE^0_{cell}$
 - $= -2 \times 96500 \times (-0.5)$
 - = 96500 J
 - = 96.5 kJ = 96500 J
- FOUNDATI 50. The number of chiral carbons present in the molecule given below is......



PART-C : MATHEMATICS

SECTION – 1 : (Maximum Marks : 80)

Single Choice Type

This section contains 20 Single choice questions. Each question has 4 choices (1), (2), (3) and (4) for its answer, out of which Only One is correct.

Full Marks : +4 If ONLY the correct option is chosen.

Negative Marks : -1 (minus one) mark will be deducted for indicating incorrect response.

51.	The sum of the first three terms of a G.P. is S and their product is 27. Then all such S lie in				
	(1) (–∞, –3] ∪ [9, ∞)	(2) (–∞, –9] ∪ [3, ∞)	(3) [−3, ∞)	(4) (-∞, 9]	
Ans.	(1)				
Sol.	Let terms are $\frac{a}{r}$,a,ar				
	then $a^3 = 27 \implies a = 3$	3			
	Now $\frac{3}{r} + 3 + 3r = S$			70,	
	$3\left(\frac{1}{r}+r\right)+3=S$				
	$r+\frac{1}{r}\geq 2$			R	
	$3\left(\frac{1}{r}+r\right)+3\in\left(-\infty,-3\right]$	(9,∞)	20		

52. Box I contains 30 cards numbered I to 30 and Box II contains 20 cards numbered 31 to 50. A box is selected at random and a card is drawn from it. The number on the card is found to be a non-prime number. The probability that the card was drawn from Box I is :

(1)
$$\frac{2}{3}$$
 (2) $\frac{2}{5}$ (3) $\frac{8}{17}$ (4) $\frac{4}{17}$

Ans. (3)

Sol. $P(B_1) = \frac{1}{2} = P(B_2)$

 $P(Non-prime) = P(B_1).P(N.P/B_1) + P(B_2).P(N.P/B_2)$

$$= \frac{1}{2} \cdot \frac{20}{30} + \frac{1}{2} \cdot \frac{15}{20}$$
$$P(B_1/N.P.) = \frac{\frac{1}{2} \cdot \frac{20}{30}}{\frac{1}{2} \cdot \frac{20}{30} + \frac{1}{2} \cdot \frac{15}{20}} = \frac{8}{17}$$

53. Area (in sq. units) of the region outside
$$\frac{|x|}{2} + \frac{|y|}{3} = 1$$
 and inside the ellipse $\frac{x^2}{4} + \frac{y^2}{9} = 1$ is
(1) $3(\pi - 2)$ (2) $3(4 - \pi)$ (3) $6(\pi - 2)$ (4) $6(4 - \pi)$
Ans. (3)
Sol. Area of Ellipse = $\pi ab = 6\pi$
Area enclose by $\frac{|x|}{2} + \frac{|y|}{3} = 1$ is
 $= \frac{1}{2}(d,d_2) = \frac{1}{2}(4)(6) = 12$
so required area is $= 6\pi - 12$
54. The domain of the function $f(x) = \sin^{-1}(\frac{|x| + 5}{x^2 + 1})$ is $(-\infty, -a] \cup [a, \infty)$
(1) $\frac{1 + \sqrt{17}}{2}$ (2) $\frac{\sqrt{17} - 1}{2}$ (3) $\frac{\sqrt{17}}{2}$ (4) $\frac{\sqrt{17}}{2} + 1$
Ans. (1)
Sol. $\frac{|x| + 5}{x^2 + 1} \le 1$
 $|x| + 5 \le x^2 + 1$
 $x^2 - |x| - 4 \ge 0$
Let $|x| = t \implies t^2 - t - 4 \ge 0$
 $\left(1 \times 1 + \frac{\sqrt{17} - 1}{2} \right) \left(|x| - \frac{\sqrt{17} + 1}{2} \right) \ge 0$
 $x \in \left(-\infty, \frac{\sqrt{17} + 1}{2} \right) \cup \left[\frac{\sqrt{17} + 1}{2}, \infty \right]$
 $a = \frac{1 + \sqrt{17}}{2}$
55. If $|x| \le 1$ by ≤ 1 and $x \ge x$ then the sum to infinity of the following series $(x + y) + (y^2 + y) + y^2$

, then the sum to infinity of the following series $(x + y) + (x^2 + xy + y^2) + (x^3 + y^2)$ $x^2y + xy^2 + y^3) + \dots$ is :

(1)
$$\frac{x+y+xy}{(1-x)(1-y)}$$
 (2) $\frac{x+y-xy}{(1-x)(1-y)}$ (3) $\frac{x+y-xy}{(1-x)(1+y)}$ (4) $\frac{x+y+xy}{(1+x)(1+y)}$

Ans. (2)

Sol.
$$(x + y) + (x^2 + xy + y^2) + (x^3 + x^2y + xy^2 + y^3) + \dots$$

$$=\frac{1}{x-y}\left(\frac{x^2}{1-x}-\frac{y^2}{1-y}\right)=\frac{1}{x-y}\left(\frac{x^2-x^2y-y^2+xy^2}{(1-x)(1-y)}\right)=\frac{x+y-xy}{(1-x)(1-y)}$$

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56. The value of
$$\left(\frac{1+\sin\frac{2\pi}{9}+\cos\frac{2\pi}{9}}{1+\sin\frac{2\pi}{9}-\cos\frac{2\pi}{9}}\right)^{3}$$
 is :
(1) $-\frac{1}{2}(\sqrt{3}-i)$ (2) $\frac{1}{2}(\sqrt{3}-i)$ (3) $\frac{1}{2}(1-i\sqrt{3})$ (4) $-\frac{1}{2}(1-i\sqrt{3})$
Ans. (1)
Sol. $\left(\frac{1+\cos\frac{5\pi}{18}+\sin\frac{5\pi}{18}}{1+\cos\frac{5\pi}{18}-\sin\frac{5\pi}{18}}\right)^{3} = \left(\frac{2\cos^{2}\frac{5\pi}{38}+12\sin\frac{5\pi}{36}\cos\frac{5\pi}{36}}{2\cos^{2}\frac{5\pi}{36}-12\sin\frac{5\pi}{36}\cos\frac{5\pi}{36}}\right)^{3}$
 $\left(\frac{\cos\frac{5\pi}{36}+i\sin\frac{5\pi}{18}}{\cos\frac{5\pi}{36}-i\sin\frac{5\pi}{36}}\right)^{2} = \left(\cos\frac{5\pi}{36}+i\sin\frac{5\pi}{6}\right)^{4}$
 $=\cos\left(6\times\frac{5\pi}{36}\right)+i\sin\left(6\times\frac{5\pi}{36}\right)=\cos\frac{5\pi}{6}+i\sin\frac{5\pi}{6}\Rightarrow-\frac{\sqrt{3}}{2}+1\frac{1}{2}$
57. Let $y = y(x)$ be the solution of the differential equation, $\frac{2+\sin x}{y+1}, \frac{dy}{dx} = -\cos x, y > 0, y(0) = 1$. If $y(\pi) = a$
and $\frac{dy}{dx}$ at $x = \pi$ is b, then the ordered pair (a, b) is equal to :
(1) $\left(2,\frac{3}{2}\right)$ (2) (1, -1) (3) (2, 1) (4) (1, 1)
Ans. (4)
Sol. $\frac{dy}{1+y} = \frac{-\cos x}{2+\sin x} dx$
 $rn(1+y) = -rn(2+\sin x) + rnc$
 $(1+y)(2+\sin x) = c$
 $4, 1 = c$ \Rightarrow $c = 4$
 $1+y = \frac{4}{2+\sin x} \Rightarrow y = \frac{4}{2+\sin x} = 1$
 $y(\pi) = 2 - 1 = 1 = a$
 $\frac{dy}{dx} = \frac{-4}{(2+\sin x)^{2}}\cos(x = 1 \text{ at } x - \pi \Rightarrow b = 1$
 $(a, b) = (1, 1)$
58. The plane passing through the points (1, 2, 1), (2, 1, 2) and parallel to the line, $2x = 3y, z = 1$ also passes through the point :
(1) $(2, 0, -1)$ (2) $(0, 6, -2)$ (3) $(0, -6, 2)$ (4) $(-2, 0, 1)$

Sol. Plane passes through (2, 1, 2) is

59.

Sol.

60.

a(x-2) + b(y-1) + (z-2) = 0it also passes through (1, 2, 1) $-a+b-c=0 \Rightarrow a-b+c=0$ *.*..(1) given line $\frac{x}{3} = \frac{y}{2} = \frac{z-1}{0}$ is parallel to (1) ÷ 3a + 2b + c0 = 0 $\frac{a}{0-2} = \frac{b}{3-0} = \frac{c}{2+3}$ $\frac{a}{2} = \frac{b}{-3} = \frac{c}{2+3}$ $\frac{a}{2} = \frac{b}{-3} = \frac{c}{-5}$ *:*.. plane is $2x - 4 - 3y + 3 - 5z + 10 = 0 \implies 2x - 3y - 5z + 9 = 0$ Let $\alpha > 0$, $\beta > 0$ be such that $\alpha^3 + \beta^2 = 4$. If the maximum value of the term independent of x in the binomial expansion of $(\alpha x^{1/9} + \beta x^{1/6})^{10}$ is 10k, then k is equal to : (1) 176 (3) 352 (4) 84 (2) 336 (2) Ans. $T_{r+1} = {}^{10}C_r(\alpha x^{1/9})^{10-r} (\beta x^{-1/6})^r$ $T_{r+1} = {}^{10}C_r \alpha^{10-r} \beta^r(x) \frac{10-r}{9} \frac{r}{6}$ Term independent of x $\frac{10-r}{9}-\frac{r}{6}=0 \Rightarrow r=4$ IT-JEE $T_5 = {}^{10}C_4 \alpha^6 \beta^4$ Let α^3 , β^2 are 2 numbers. Now $A \ge G$ $\frac{\alpha^3+\beta^2}{2} \ge (\alpha^3\beta^2)^{1/2}$ \Rightarrow $\alpha^3 \beta^2 \le 4$ \Rightarrow $\alpha^6 \beta^4 \le 16$ \Rightarrow ≤ 6 \Rightarrow 10C $T_5 \le 16. \ ^{10}C_4$ \Rightarrow $T_{5 max} = 16 \times {}^{10}C_4 = 10 K$ \Rightarrow K = 336 \Rightarrow If R = {(x, y) : x, y, \in Z, x² + 3y² \leq 8} is a relation on the set of integers Z, then the domain R⁻¹ is : $(1) \{-1, 0, 1\}$ $(2) \{-2, -1, 1, 2\}$ $(3) \{0, 1\}$ $(4) \{-2, -1, 0, 1, 2\}$ (1) Ans.





Domain of $R^{-1} \equiv Range$ of $R \equiv Value$ of $y \equiv \{-1, 0, 1\}$

(2) - 12

61. If p(x) be a polynomial of degree three that has a local maximum value 8 at x = 1 and a local minimum value 4 at x = 2; then p(0) is equal to

(3) 6

+ C = 8

(4) 12

....(i)

....(ii)

Ans. (2)

(1) - 24

Sol. Clearly
$$P'(x) = \lambda (x - 1) (x - 2)$$
 where $\lambda > 0$

$$\mathsf{P}(\mathsf{x}) = \lambda \left[\frac{\mathsf{x}^3}{3} - \frac{3\mathsf{x}^2}{2} + 2\mathsf{x} \right] + \mathsf{C}$$

given P(1) = 8 $\Rightarrow \lambda \left(\frac{1}{3} - \frac{3}{2} + 2\right) + C = 8$ also P(2) = 4 $\Rightarrow \lambda \left(\frac{8}{3} - 6 + 4\right) + C = 4$

By (i) and (ii) \Rightarrow C = -12 \Rightarrow P(0) = -12

62. A line parallel to the straight line 2x - y = 0 is tangent to the hyperbola $\frac{x^2}{4} - \frac{y^2}{2} = 1$ at the point (x_1, y_1) .

Then $x_1^2 + 5y_1^2$ is equal to :

(1) 10 (2) 5 (3) 8 (4) 6

And. (4)

_

Sol. Tangent at (x_1, y_1)

 $xx_1 - 2yy_1 - 4 = 0$ This is parallel to 2x - y =

$$\Rightarrow \frac{x_1}{2y_1} = 2$$

$$\Rightarrow \qquad x_1 = 4y_1 \qquad \dots (1)$$

Point (x_1, y_1) lie on hyperbola.

$$\frac{x_1^2}{4} - \frac{x_1^2}{2} - 1 = 0 \quad \dots (2)$$

On solving eq. (1) and (2) We get $x_1^2 + 5y_1^2 = 6$ 63. The contrapositive of the statement "If I reach the station in time, then I will catch the train" is: (1) If I will catch the train, then I reach the station in time. (2) If do not reach the station in time, then I will not catch the train. (3) If I do not reach the station in time, then I will catch the train. (4) If I will not catch the train, then I do not reach the station in time. Ans. (4) Sol. Contrapositive of $p \rightarrow q$ is $\sim q \rightarrow \sim p$ 64. Let P(h, k) be a point on the curve $y = x^2 + 7x + 2$, nearest to the line, y = 3x - 3. Then the equation of the normal to the curve at P is : $(2) x + 3y + 26 = 0 \qquad (3) x - 3y - 11 = 0 \qquad (4) x - 3y + 22 = 0$ (1) x + 3y - 62 = 0Ans. (2) Common normal Tangent at p(h, k) will be parallel to given line $\frac{dy}{dx}\Big|_{(h,k)} = 2h + 7 = 3$ Sol. y=3k-3 h = -2 \Rightarrow Point P lies on curve K = $(-2)^2 - 7 \times 2 + 2 = -8$ P(h,k) Normal at P(-2, -8), normal slop = $-\frac{1}{2}$ x + 3y + 26 = 0Let A be a 2 × 2 real matrix with entries from {0, 1} and $|A| \neq 0$. Consider the following two statements ; 65. (P) If $A \neq I_2$, then |A| = -1(Q) If |A| = 1, then tr(A) = 2 where I_2 denotes 2 × 2 identity matrix and tr(A) denotes the sum of the diagonal entries of A. Then : (1) (P) is true and (Q) are false (2) Both (P) and (Q) are true (3) Both (P) and (Q) are false (4) (P) is false and (Q) is true Ans. (2) Let $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ Sol. a, b, c, d ∈ {0, 1} $|A| = ad - bc \neq 0$ ad = 1, bc = 0 or ad = 0, bc = 1 \Rightarrow If $A \neq I_2 \implies ad \neq 1 \implies$ ad = 0, bc = 1 \Rightarrow |A| = -1(P) (P) is true. (Q) If $A = I \implies$ ad = 1 \Rightarrow ad = 1, bc = 0 \Rightarrow tr(A) = 2 (Q) is true. 66. Let S be the set of all $\lambda \in R$ for which the system of linear equations 2x - y + 2z = 2 $x - 2y + \lambda z = -4$ $x + \lambda y + z = 4$

has no solution. then the set S

(1) is a singleton (2) contains exactly two elements (3) contains more than two elements (4) is an empty set Ans. (2)Sol. For no. solution Δ = 0 and at least one of Δ_1 , Δ_2 , Δ_3 is non-zero. $\Delta = \begin{vmatrix} 2 & -1 & 2 \\ 1 & -2 & \lambda \\ 1 & \lambda & 1 \end{vmatrix} = (\lambda - 1)(2\lambda + 1)$ $\Delta_{1} = \begin{vmatrix} 2 & -1 & 2 \\ -4 & -2 & \lambda \\ 4 & \lambda & 1 \end{vmatrix} = -2(\lambda^{2} + 6\lambda - 4)$ $\Delta = 0 \implies \lambda = 1, -\frac{1}{2}$ Hence, $S = \left\{1, -\frac{1}{2}\right\}$ If the tangent to the curve $y = x + \sin y$ at a point (a, b) is parallel to the line joining $\left(0, \frac{3}{2}\right)$ and $\left(\frac{1}{2}, 2\right)$, 67. then (4) b = a (1) |b-a| = 1 (2) $b = \frac{\pi}{2} + a$ (3) |a + b| = 1 Ans. (1)Sol. y = x + siny $\frac{dy}{dx} = \frac{1}{1 - \cos y} = \frac{\frac{1}{2} - 0}{2 - \frac{3}{2}} = 1$ \Rightarrow $\cos y = 0$ \Rightarrow Point lie on curve b = a + sin y b - a = sin y|b – a| = 1 68. If a function f(x) defined by $f(x) = \begin{cases} ae^{x} + be^{-x} \ , \ -1 \leq x < 1 \\ cx^{2} \ , \ 1 \leq x \leq 3 \end{cases}$ $ax^2 + 2cx$, $3 < x \leq 4$ be continuous for some a, b, c \in R and f'(0) + f'(2) = e, then the value of a is : (1) $\frac{1}{e^2 - 3e + 13}$ (2) $\frac{e}{e^2 - 3e + 13}$ (3) $\frac{e}{e^2 - 3e - 13}$ (4) $\frac{e}{e^2 + 3e + 13}$ Ans. (2) Sol. Continuous at x = 1, 3 $f(1) = f(1^+) \implies ae + be^{-1} = c$(1)

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 $f(3) = f(3^+)$ $9c = 9a + 6c \implies c = 3a$ \Rightarrow(2) From (1) and (2) b = ae(3 - e)....(3) _____ax^x − be^{-x} −1 < x < 1 $f'(x) = \begin{vmatrix} 2cx & 1 < x < 3 \end{vmatrix}$ 2ax + 2c3 < x < 4 f'(0) = a - b, f'(2) = 4cGiven f'(0) + f'(2) = ea - b + 4c = e....(4) by using eq. (1), (2), (3) & (4) $a = \frac{e}{e^2 - 3e + 13}$ 69. Let α and β be the roots of the equation, $5x^2 + 6x - 2 = 0$. If $S_n = \alpha^n + \beta^n$, $n = 1, 2, 3, \dots$, then : (1) 6S6 + 5S5 = 2S4 (2) 5S6 + 6S5 = 2S4 (3) 5S6 + 6S5 + 2S4 = 0 (4) 6S6 + 5S5 + 2S4 = 0 Ans. (2)Sol. $5\alpha^2 + 6\alpha = 2$ $5S_6 + 6S_5 = \alpha^4(5\alpha^2 + 6\alpha) + \beta^4(5\beta^2 + 6\beta)$ $= 2(\alpha^4 + \beta^4) = 2S_4$ Let X = {x \in N : 1 \leq 1 \leq 17} and Y = {ax + b : x \in X and a, b \Box R, a > 0}. If mean and variance of elements 70. of Y are 17 and 216 respectively then a + b is equal to : (3) –7 (4) –27 (1)7(2)9(3) Ans. B(\bar{x}) = a \bar{x} + b = $\frac{a(1+2+3+...+17)}{17}$ + b = 17 b Sol. $\frac{a.(17.18)}{17.2} + b = 17$ 9a + b = 17 $\sigma A^{2} = \frac{\sum x^{2}}{n} - \left(\frac{\sum x}{n}\right)^{2} = \frac{1^{2} + 2^{2} + \dots + 17^{2}}{17} - \left(\frac{1 + 2 + \dots + 17}{17}\right)^{2}$ $=\frac{17.18.35}{6.17}-\left(\frac{17.18}{2.17}\right)$ = 105 - 81 = 24 $\therefore \sigma_{B}^{2} = a^{2}\sigma_{A}^{2} = a^{2}.24 = 216$ $a^2 = \frac{216}{24} = 9$ a=3 ∴ b=17–27 ∴ b = 17 – 27 b = -10∴ a+b=-7

	This section contains FIVE (05) questions. The answer to each question is NUMERICAL VALUE with			
	two digit integer and decimal upto one digit.			
	If the numerical value has more than two decimal places truncate/round-off the value upto TWO decimal places.			
	Full Marks : +4 If ONLY the correct option is chosen.			
	Zero Marks : 0 In all other cases			
71.	Let \vec{a}, \vec{b} and \vec{c} three unit vectors such that $ \vec{a} - \vec{c} ^2 + \vec{a} - \vec{c} ^2 = 8$. Then $ \vec{a} + 2\vec{b} ^2 + \vec{a} + 2\vec{c} ^2$ is equal			
	to			
Ans.	(02.00)			
Sol.	ā = b = c = 1			
	$ \vec{a} - \vec{b} ^2 + \vec{a} - \vec{c} ^2 = 8$			
	$\Rightarrow \vec{a} \cdot \vec{b} + \vec{a} \cdot \vec{c} = -2$			
	Now $ \vec{a}+2\vec{b} ^2 + \vec{a}+2\vec{c} ^2 = 2 \vec{a} ^2 + 4 \vec{b} ^2 + 4 \vec{c} + 4(\vec{a}\cdot\vec{b}+\vec{a}\cdot\vec{c}) = 2$			
72.	If $\lim_{x \to 1} \frac{x + x^2 + x^3 + \dots + x^n - n}{x - 1} = 820, (n \in \mathbb{N})$ then the value of n is equal to			
Ans.	(40.00)			
Sol.	$\lim_{x \to 1} \frac{x + x^2 + x^3 + \dots + x^n - n}{x - 1} = 820 \left(\frac{0}{0}\right)$			
	$\lim_{x \to 1} \frac{1 + 2x + 3x^2 + \dots \cdot nx^{n-1}}{1} = 820$			
	\Rightarrow 1 + 2 + 3 + n = 820			
	$\Rightarrow \frac{n(n+1)}{2} = 820$			
	$\Rightarrow n^2 + n - 1640$			
	$\Rightarrow n^2 + n - 1640 = 0$			
	\Rightarrow n = 40 n \in N			
73.	The number of integral values of k for which the line, $3x + 4y = k$ intersects the circle, $x^2 + y^2 - 2x - 4y + y^2 + 2x + 4y + y^2 + 4y + y^2 + 4y + y^2 + 2x + 4y + y^2 + 4y + 4$			
	4 = 0 at two distinct points is			
Ans.	(09.00)			

SECTION – 2 : (Maximum Marks : 20)

Sol. If line cuts circle then p < r

Centre of circle
$$(1, 2)$$
, r = 1

$$\frac{3+8-k}{5} < 1 \implies k \in (6,16)$$

 $k=7,\,8,\,9,\,10,\,11,\,12,\,13,\,14,\,15,\,\ldots\ldots$

74. If the letters of the word 'MOTHER' be permuted and all the words so formed (with or without meaning) be listed as in a dictionary, then the position of the word 'MOTHER' is

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Sol. MOTHER 346215 \Rightarrow 251+241+331+21+1=240+48+18+2+1=309 75. The integral $\int_{0}^{2} x-1 -x dx$ is equal to : Ans. (01.50) Sol. $\int_{0}^{2} x-1 -x dx = \int_{0}^{1} 1-x-x dx + \int_{1}^{2} x-1-x dx$ $= \int_{0}^{1/2} (1-2x) dx + \int_{1/2}^{1} (2x-1) dx + \int_{1}^{2} dx$ $= [x-x]_{0}^{\frac{1}{2}} + [x^{2} - x]_{\frac{1}{2}}^{0} + [x]_{1}^{2} = \frac{1}{2} - \frac{1}{4} + (1-1) - (\frac{1}{4} - \frac{1}{2}) + 2 - 1 = \frac{1}{4} + \frac{1}{4} + 1 = \frac{3}{2}$	Ans.	(309.00)
3 4 6 2 1 5 \Rightarrow 2 5 + 2 4 + 3 3 + 2 + 1 = 240 + 48 + 18 + 2 + 1 = 309 75. The integral $\int_{0}^{2} x - 1 - x dx$ is equal to : Ans. (01.50) Sol. $\int_{0}^{2} x - 1 - x dx = \int_{0}^{1} 1 - x - x dx + \int_{1}^{2} x - 1 - x dx$ $= \int_{0}^{\frac{1}{2}} (1 - 2x) dx + \int_{\frac{1}{2}}^{1} (2x - 1) dx + \int_{1}^{2} dx$ $= [x - x]_{0}^{\frac{1}{2}} + [x^{2} - x]_{\frac{1}{2}}^{0} + [x]_{1}^{2} = \frac{1}{2} - \frac{1}{4} + (1 - 1) - (\frac{1}{4} - \frac{1}{2}) + 2 - 1 = \frac{1}{4} + \frac{1}{4} + 1 = \frac{3}{2}$	Sol.	MOTHER
75. The integral $\int_{0}^{1} x-1 -x dx$ is equal to : Ans. (01.50) Sol. $\int_{0}^{2} x-1 -x dx = \int_{0}^{1} 1-x-x dx + \int_{1}^{2} x-1-x dx$ $= \int_{0}^{1/2} (1-2x) dx + \int_{1/2}^{1} (2x-1) dx + \int_{1}^{2} dx$ $= [x-x]_{0}^{\frac{1}{2}} + [x^{2}-x]_{\frac{1}{2}}^{0} + [x]_{1}^{2} = \frac{1}{2} - \frac{1}{4} + (1-1) - (\frac{1}{4} - \frac{1}{2}) + 2 - 1 = \frac{1}{4} + \frac{1}{4} + 1 = \frac{3}{2}$		$3 \ 4 \ 6 \ 2 \ 1 \ 5 \qquad \Rightarrow \qquad 2 \ 5! \ + \ 2 \ 4! \ + \ 3 \ 3! \ + \ 2! \ + \ 1 \ = \ 240 \ + \ 48 \ + \ 18 \ + \ 2 \ + \ 1 \ = \ 309$
Ans. (01.50) Sol. $\int_{0}^{2} x-1 - x dx = \int_{0}^{1} 1-x-x dx + \int_{1}^{2} x-1-x dx$ $= \int_{0}^{1/2} (1-2x) dx + \int_{1/2}^{1} (2x-1) dx + \int_{1}^{2} dx$ $= [x-x]_{0}^{\frac{1}{2}} + [x^{2}-x]_{\frac{1}{2}}^{0} + [x]_{1}^{2} = \frac{1}{2} - \frac{1}{4} + (1-1) - (\frac{1}{4} - \frac{1}{2}) + 2 - 1 = \frac{1}{4} + \frac{1}{4} + 1 = \frac{3}{2}$	75.	The integral $\int_{0}^{2} x-1 -x dx$ is equal to :
Sol. $\int_{0}^{1} x-1 -x dx = \int_{0}^{1} 1-x-x dx + \int_{1}^{2} x-1-x dx$ $= \int_{0}^{1/2} (1-2x) dx + \int_{1/2}^{1} (2x-1) dx + \int_{1}^{2} dx$ $= [x-x]_{0}^{\frac{1}{2}} + [x^{2}-x]_{0}^{\frac{1}{2}} + [x]_{1}^{2} = \frac{1}{2} - \frac{1}{4} + (1-1) - (\frac{1}{4} - \frac{1}{2}) + 2 - 1 = \frac{1}{4} + \frac{1}{4} + 1 = \frac{3}{2}$	Ans.	(01.50)
$= \int_{0}^{1/2} (1-2x) dx + \int_{1/2}^{1} (2x-1) dx + \int_{1}^{2} dx$ $= [x-x]_{0}^{\frac{1}{2}} + [x^{2}-x]_{\frac{1}{2}}^{0} + [x]_{1}^{2} = \frac{1}{2} - \frac{1}{4} + (1-1) - (\frac{1}{4} - \frac{1}{2}) + 2 - 1 = \frac{1}{4} + \frac{1}{4} + 1 = \frac{3}{2}$	Sol.	$\int_{0}^{2} x-1 - x dx = \int_{0}^{1} 1-x-x dx + \int_{1}^{2} x-1-x dx$
$= [x - x]_0^1 + [x^2 - x]_{\frac{1}{2}}^0 + [x]_1^2 = \frac{1}{2} - \frac{1}{4} + (1 - 1) - (\frac{1}{4} - \frac{1}{2}) + 2 - 1 = \frac{1}{4} + \frac{1}{4} + 1 = \frac{3}{2}$		$=\int_{0}^{1/2}(1-2x)dx+\int_{1/2}^{1}(2x-1)dx+\int_{1}^{2}dx$
FOUNDATIO		$= \left[x - x\right]_{0}^{\frac{1}{2}} + \left[x^{2} - x\right]_{\frac{1}{2}}^{0} + \left[x\right]_{1}^{2} = \frac{1}{2} - \frac{1}{4} + (1 - 1) - \left(\frac{1}{4} - \frac{1}{2}\right) + 2 - 1 = \frac{1}{4} + \frac{1}{4} + 1 = \frac{3}{2}$
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